

## Field of the Invention

The present invention relates to radars detecting targets by transmitting and receiving radio waves obtained by performing frequency modulation on continuous waves.

## Background of the Invention

FM-CW radars utilizing millimeter waves have been developed, for example, as in-vehicle radars. FM-CW radars detect targets by transmitting and receiving radio waves obtained by performing frequency modulation (FM) on continuous waves (CW). In other words, FM-CW radars transmit a transmission signal repeating an upstream-modulation section in which a frequency gradually increases and a downstream-modulation section in which the frequency gradually decreases, receive a reception signal including a reflection signal from a target, and calculate the relative distance and the relative speed of the target in accordance with a frequency spectrum of a beat signal, which is a signal indicating the frequency difference between the transmission signal and the reception signal. Since, normally, the relative position and relative speed of a target is not constant, the above-mentioned operations are repeated at a constant frequency in order to acquire the relative position and relative speed of the target every time the operations are performed. Since targets are

distributed within a detection azimuth range, directions of the targets within the detection azimuth range can be calculated by performing the above-mentioned operations for a beam facing toward a predetermined direction and by sequentially changing the beam direction.

When a single target exists, a single projecting portion appears in a frequency spectrum of a beat signal based on a reflection wave from a target in each of an upstream-modulation section and a downstream-modulation section. Thus, the peak frequency of the projecting portion of each of the beat signal in the upstream-modulation section (hereinafter, referred to as an "upbeat signal") and the beat signal in the downstream-modulation section (hereinafter, referred to as a "downbeat signal") is calculated, and the relative distance and the relative speed of the target are calculated from the two peak frequencies.

However, when a plurality of targets exists in substantially the same direction, a plurality of projecting portions appears in a frequency spectrum of each of an upbeat signal and a downbeat signal of an identical beam. Thus, it is necessary to determine, from among the plurality of projecting portions, which combination of projecting portions is generated due to the existence of an identical target (hereinafter, referred to as "pairing"). However, as the number of detected projecting portions increases, it

takes a longer time to perform pairing. In addition, since the number of combinations increases, there is a larger possibility to perform wrong pairing. Thus, there are a problem in that the number of targets that can be detected within a limited period of time is limited, a problem in that providing an arithmetic processing unit capable of performing a high-speed arithmetic operation in order to detect many targets increases cost, and a problem in that it is difficult to acquire accurate relative distance and speed when wrong pairing is performed.

In order to avoid the above-described problems, actual radars increase the accuracy by performing filtering processing in which context is taken into consideration so as not to depend only on a single pairing operation. However, it is important not to perform wrong pairing from the beginning.

Thus, as disclosed in patent document 1, pairing is performed by regarding a combination of projecting portions appearing in a frequency spectrum of a reception signal, intensities of the projecting portions being substantially equal to each other, as being caused by an identical target.

In addition, a technology for setting the gradient of upstream modulation and the gradient of downstream modulation such that a moving distance by the amount corresponding to a Doppler shift frequency corresponds to a

moving distance by relative speed at a predicted time in the future is disclosed in patent document 2. With this arrangement, distance can be calculated without performing pairing.

Patent Document 1: Japanese Unexamined Patent  
Application Publication No. 4-343084

Patent Document 2: Japanese Unexamined Patent  
Application Publication No. 6-94829

However, in the method described in patent document 1, if a plurality of projecting portions whose reception signal intensities are substantially equal to each other appears, a combination of a pair of projecting portions may not be determined.

In addition, in the method described in patent document 2, although pairing is not necessary for calculating distance, relative speed cannot be calculated.

#### Summary of the Invention

Thus, it is an object of the present invention to solve the problems mentioned above and to provide a radar that is capable of performing pairing easily and calculating relative speed.

In a radar that transmits a transmission signal alternately repeating an upstream-modulation section in which a frequency gradually increases and a downstream-modulation section in which the frequency gradually

decreases, that receives a reception signal serving as a reflection signal of the transmission signal reflected from a target, that acquires data on a frequency spectrum of a beat signal for the transmission signal and the reception signal, that performs pairing, from among a plurality of first projecting portions appearing in the frequency spectrum of the beat signal in the upstream-modulation section and a plurality of second projecting portions appearing in the frequency spectrum of the beat signal in the downstream-modulation section, and that detects a relative distance and a relative speed in accordance with frequencies of two projecting portions forming the pair, a center frequency (that is, a component based on a range delay) of peak frequencies of first and second projecting portions at a timing a certain period of time after a predetermined timing is predicted in accordance with a peak frequency of a first projecting portion at the predetermined timing, and a pair of projecting portions acquired at the timing after the certain period of time is extracted in accordance with the center frequency.

In addition, a center frequency of peak frequencies of first and second projecting portions at a timing a certain period of time before a predetermined timing is predicted in accordance with a peak frequency of a second projecting portion at the predetermined timing, and a pair of

projecting portions acquired at the timing before the certain period of time is extracted in accordance with the center frequency.

In addition, the pair of projecting portions is extracted by using, as the certain period of time,  $nT$  satisfying a relationship,  $nT \approx f_0 / (2\Delta F \cdot f_m)$  (here,  $n$  represents a desired natural number), where  $T$  represents a measurement cycle in which the frequency analysis is performed,  $1/f_m$  represents a modulation cycle serving as a cycle including the upstream-modulation section and an adjacent downstream-modulation section,  $f_0$  represents a center frequency of the transmission signal, and  $\Delta F$  represents a width of a frequency shift in the upstream-modulation section and the downstream-modulation section.

In addition, a center frequency of peak frequencies of first and second projecting portions at a predetermined timing is predicted by using a peak frequency of a first projecting portion at a timing a certain period of time before the predetermined timing and a peak frequency of a second projecting portion at a timing the certain period of time after the predetermined timing, and a pair of projecting portions acquired at the predetermined timing is extracted in accordance with the center frequency.

When a second projecting portion forming a pair with the first projecting portion at the timing before the

certain period of time that is used for predicting the center frequency at the predetermined timing and that exhibits a frequency difference substantially equal to a difference between the peak frequencies of the first and second projecting portions forming the pair at the predetermined timing does not exist and/or when a first projecting portion forming a pair with the second projecting portion at the timing after the certain period of time that is used for predicting the center frequency at the predetermined timing and that exhibits the frequency difference does not exist, a combination of the first and second projecting portions at the predetermined timing is excluded from pair candidates.

A center frequency (that is, a component based on a range delay) of peak frequencies of first and second projecting portions at a timing a certain period of time after a predetermined timing is predicted in accordance with a peak frequency of a first projecting portion at the predetermined timing, and a pair of projecting portions acquired at the timing after the certain period of time is extracted in accordance with the center frequency. Thus, pairing can be performed easily, and it is less likely to cause wrong pairing. Therefore, relative distance and speed can be calculated accurately. In addition, since the amount of calculation necessary for pairing is reduced, the number

of targets that can be detected per unit time is increased. Thus, a cycle of detection can be shortened.

In addition, a center frequency (that is, a component based on a range delay) of peak frequencies of first and second projecting portions at a timing a certain period of time before a predetermined timing is predicted in accordance with a peak frequency of a second projecting portion at the predetermined timing, and a pair of projecting portions acquired at the timing before the certain period of time is extracted in accordance with the center frequency. Thus, pairing can be performed easily, and it is less likely to cause wrong pairing. Therefore, relative distance and speed can be calculated accurately. In addition, since the amount of calculation necessary for pairing is reduced, the number of targets that can be detected per unit time is increased. Thus, a cycle of detection can be shortened.

In addition, the pair of projecting portions at the predetermined timing is extracted by using, as the certain period of time,  $nT$  satisfying a relationship,  $nT \approx f_0 / (2\Delta F \cdot f_m)$  in which  $n$  represents a desired natural number, where  $T$  represents a measurement cycle,  $1/f_m$  represents a modulation cycle serving as a cycle including the upstream-modulation section and an adjacent downstream-modulation section,  $f_0$  represents a center frequency of the



transmission signal, and  $\Delta F$  represents a width of a frequency shift in the upstream-modulation section and the downstream-modulation section. Thus, the pair of projecting portions acquired at the predetermined timing can be extracted from a peak frequency of a first projecting portion at measurement  $n$  times before the predetermined timing or from a peak frequency of a second projecting portion at measurement  $n$  times after the predetermined timing.

In addition, a center frequency of peak frequencies of first and second projecting portions at a predetermined timing is predicted by using a peak frequency of a first projecting portion at a timing a certain period of time before the predetermined timing and a peak frequency of a second projecting portion at a timing the certain period of time after the predetermined timing, and a pair of projecting portions acquired at the predetermined timing is extracted in accordance with the center frequency. Thus, even in a case where the relationship  $nT \approx f_0 / (2\Delta F \cdot f_m)$  is not satisfied or even in a case where an error occurs from the relationship, a predicted error of a center frequency is canceled. Thus, the accuracy of pairing can be increased.

When a second projecting portion forming a pair with the first projecting portion at the timing before the certain period of time that is used for predicting the

center frequency of the peak frequencies of the first and second projecting portions at the predetermined timing and that exhibits a frequency difference substantially equal to a difference between the peak frequencies of the first and second projecting portions forming the pair at the predetermined timing does not exist and/or when a first projecting portion forming a pair with the second projecting portion at the timing after the certain period of time that is used for predicting the center frequency at the predetermined timing and that exhibits the frequency difference does not exist, a combination of the first and second projecting portions at the predetermined timing is excluded from pair candidates. Thus, the number of pair candidates can be reduced quickly, and pairing can be performed more quickly. In addition, it is less likely to cause wrong pairing.

#### Brief Description of the Drawings

Fig. 1 is a block diagram showing a structure of a radar.

Fig. 2 illustrates an example of beat signals in an upstream-modulation section and a downstream-modulation section of the radar.

Fig. 3 illustrates an example of frequency spectra of beat signals in an upstream-modulation section and a downstream-modulation section.

Fig. 4 illustrates examples of changes of peak frequencies and the like at various timings of a radar according to a first embodiment.

Fig. 5 illustrates examples of changes of peak frequencies and the like at various timings of the radar according to the first embodiment.

Fig. 6 is a flowchart showing a processing procedure for pairing performed by the radar.

Fig. 7 is a flowchart showing a processing procedure for pairing performed by a radar according to a second embodiment.

Fig. 8 illustrates examples of changes of peak frequencies and the like at various timings of a radar according to a third embodiment.

Fig. 9 is a flowchart showing a processing procedure for pairing performed by the radar.

#### Reference Numerals

- 1 - RF block
- 2 - signal processing block
- 3 - dielectric lens
- 4 - primary radiator
- 5 - circulator
- 6 - coupler
- 7 - isolator
- 8 - VCO

- 9 - mixer
- 13 - digital signal processor
- 14 - microprocessor
- 16 - scan unit

#### Detailed Description of the Invention

Fig. 1 is a block diagram showing the structure of a radar according to an embodiment of the present invention.

As shown in Fig. 1, the radar includes an RF block 1 and a signal processing block 2. The RF block 1 transmits and receives radio waves for radar measurement and outputs to the signal processing block 2 beat signals with respect to transmission waves and reception waves. A modulation counter 11 of the signal processing block 2 performs counting to cause a DA converter 10 to generate a triangular wave signal, and outputs the counted value to the DA converter 10. The DA converter 10 converts the counted value into an analog voltage signal, and supplies the analog voltage signal to a VCO (voltage controlled oscillator) 8 of the RF block 1. Then, FM modulation is performed on transmission waves. In other words, an oscillation signal of the VCO 8 is supplied to a primary radiator 4 via an isolator 7, a coupler 6, and a circulator 5. The primary radiator 4 is disposed on a focal plane of a dielectric lens 3 or in a position near the focal plane. The dielectric lens 3 transmits, as a sharp beam, a millimeter wave signal

emitted from the primary radiator 4. When a reflection wave from a target (a vehicle or the like) enters the primary radiator 4 via the dielectric lens 3, a reception signal is guided to a mixer 9 via the circulator 5. The reception signal and a local signal, which is a part of a transmission signal from the coupler 6, are input to the mixer 9. The mixer 9 outputs, as an intermediate-frequency signal, a beat signal corresponding to a signal indicating the frequency difference between the reception signal and the local signal to an AD converter 12 of the signal processing block 2. The AD converter 12 converts the intermediate-frequency signal into digital data. A DSP (digital signal processor) 13 performs FFT (fast Fourier transform) on a data string input from the AD converter 12, and calculates the relative distance and the relative speed of the target, as described later.

A scan unit 16 in the RF block 1 performs parallel displacement of the primary radiator 4 on a focal plane of the dielectric lens 3 or on a plane parallel to the focal plane. A 0 dB coupler is formed between a movable portion in which the primary radiator 4 is provided and a fixed portion. A motor M is a driving motor for the scan unit 16. The motor performs beam scanning over a range between -10 degrees and +10 degrees in a cycle of, for example, 100 milliseconds.

A microprocessor 14 in the signal processing block 2 controls the modulation counter 11 and the scan unit 16. The microprocessor 14 controls a beam direction to be set to a predetermined angle with respect to the scan unit 16 and controls the modulation counter 11 to cause the VCO 8 to perform modulation using a triangular wave. The microprocessor 14 extracts a pair (pairing) of a projecting portion appearing in a frequency spectrum in an upstream-modulation section and a projecting portion appearing in a frequency spectrum in a downstream-modulation section that are calculated by the DSP 13. In addition, the microprocessor 14 calculates the relative distance and the relative speed of a target in accordance with a method, which will be described later, and outputs the calculated relative distance and relative speed to a host apparatus, which is not shown in the drawing.

Fig. 2 shows an example of a difference between a frequency change of a transmission signal and a frequency change of a reception signal, the difference being caused by the distance to a target and a relative speed. A transmission signal TXS is a signal on which frequency modulation is performed so as to be in a triangular waveform in which a center frequency  $f_0$  is the center of the frequency. The frequency difference between the transmission signal TXS and a reception signal RXS when the

frequency of the transmission signal TXS increases is equal to a frequency  $f_1$  of an upbeat signal, and the frequency difference between the transmission signal TXS and the reception signal RXS when the frequency of the transmission signal TXS decreases is equal to a frequency  $f_2$  of a downbeat signal. Here,  $\Delta F$  represents the width of a frequency shift. The difference  $\Delta t$  on the time axis (time difference) between the triangular waveform of the transmission signal TXS and the triangular waveform of the reception signal RXS corresponds to a period of time necessary for a radio wave to go back and forth between an antenna and the target. The difference on the frequency axis between the transmission signal TXS and the reception signal RXS is equal to the amount of Doppler shift, and the difference is caused by the relative speed of the target with respect to the antenna. The time difference and the amount of Doppler shift change the frequency  $f_1$  of the upbeat signal and the frequency  $f_2$  of the downbeat signal. The distance from the radar to the target and the relative speed of the target with respect to the radar are calculated by detecting the frequencies  $f_1$  and  $f_2$ . In other words, when  $f_r$  represents a frequency component based on a range delay and  $f_d$  represents a Doppler shift frequency component based on relative speed, the following relationship is achieved:

$$f_r = (f_1 + f_2) / 2 \dots (1)$$

$$f_d = (f_2 - f_1) / 2 \dots (2).$$

Fig. 3 shows an example of a frequency spectrum of a beat signal in each of an upstream-modulation section and a downstream-modulation section. In this example, the solid line represents the frequency spectrum of the beat signal in the upstream-modulation section, and the broken line represents the frequency spectrum of the beat signal in the downstream-modulation section. In the frequency range shown in Fig. 3, three projecting portions, that is, peak frequencies  $f_{11}$ ,  $f_{12}$ , and  $f_{13}$ , appear in the beat signal in the upstream-modulation section, and two projecting portions, that is, peak frequencies  $f_{21}$  and  $f_{22}$ , appear in the beat signal in the downstream-modulation section. Pairing is performed for a plurality of projecting portions. Using a pair of peak frequencies, the relative distance to a target is calculated in accordance with condition (1), and the relative speed of the target is calculated in accordance with condition (2). For example, when the peak frequencies  $f_{13}$  and  $f_{22}$  are regarded as forming a pair, a frequency component  $f_r$  based on a range delay is calculated from the condition  $f_r = (f_{13} + f_{22}) / 2$ , and a Doppler shift frequency component  $f_d$  by a speed difference is calculated from the condition  $f_d = (f_{22} - f_{13}) / 2$ .

As shown in Fig. 2, when  $f_0$  represents a transmission



center frequency,  $1/f_m$  represents a modulation cycle,  $\Delta F$  represents the width of a frequency shift, if a target at a distance  $R$  approaches at a relative speed  $V$ , a range delay component  $f_r$  included in beat signals is represented by the relationship:

$$f_r = (4f_m \Delta F \cdot R) / C \cdots (3).$$

Thus, the distance  $R$  is calculated from the condition:

$$R = C f_r / (4f_m \Delta F) \cdots (4).$$

In addition, a frequency component  $f_d$  based on a Doppler shift included in beat signals is represented by the relationship:

$$f_d = (2V f_o) / C \cdots (5).$$

Thus, the relative speed  $V$  is calculated from the condition:

$$V = C f_d / (2f_o) \cdots (6).$$

In addition, the frequency resolution of FFT performed in each of the upstream-modulation section and the downstream-modulation section is  $2f_m$ , which is the fundamental frequency of each of the sections. When  $\delta R$  represents a corresponding range resolution and  $\delta V$  represents a corresponding speed resolution, by substituting conditions  $R = \delta R$ ,  $f_r = 2f_m$ ,  $V = \delta V$ , and  $f_d = 2f_m$  for conditions (4) and (6), the following conditions are obtained:

$$\delta R = C / 2\Delta F \cdots (7); \text{ and}$$

$$\delta V = f_m \cdot C / f_o \cdots (8).$$

The upbeat frequency  $f_1$  and the downbeat frequency  $f_2$  are represented as follows:

$$f_1 = f_r - f_d \cdots (9); \text{ and}$$

$$f_2 = f_r + f_d \cdots (10).$$

Thus, when  $\tau$  represents the time represented by the following relationship, if a target performs linear motion with constant velocity, frequencies  $f_1$  and  $f_2$  obtained at a certain time correspond to a frequency  $f_r$  at a time  $\tau$  after or  $\tau$  before the corresponding time.

$$\tau = \delta R / \delta V = f_o / (2f_m \Delta F) \cdots (11)$$

This relationship will be explained with reference to Figs. 4 and 5.

When a measurement cycle  $T$  is set so as to satisfy the relationship  $nT = \tau$ , a frequency component  $f_r$  based on a range delay of a target at a measurement timing after measurement is performed  $n$  times can be predicted at a desired timing. For example, a frequency component  $f_r$  at time  $t$  is equal to a beat frequency  $f_1$  in an upstream-modulation section at time  $t - nT$ .

Thus, processing of "calculating a distance by always regarding  $f_1$   $n$  times before as  $f_r$  at the current time" is considered. However, the relative speed of a target cannot be calculated by only this processing. In addition, when the target suddenly accelerates or decelerates or when a difference from a condition  $nT \approx \tau$  increases, an error in

distance measurement correspondingly increases.

In contrast, as described above, normal FMCW radars are capable of acquiring relative distance and relative speed at the same time by pairing beat frequencies  $f_1$  and  $f_2$  in an upstream-modulation section and a downstream-modulation section obtained by measurement at a certain time. However, if a plurality of targets exists, a plurality of frequencies  $f_1$  and  $f_2$  exist. Thus, if pairing is not performed accurately, a distance and a speed that are completely different from true values may be output.

The present invention calculates the distance and relative speed of a target in accordance with the procedure described below and solves all the above-mentioned problems at the same time.

(1) A beat frequency  $f_1$  in an upstream-modulation section at time  $t-nT$  is set as a predicted distance  $f_{1prd}$  at time  $t$ .

(2) From among beat frequencies  $f_1$  and  $f_2$  in an upstream-modulation section and a downstream-modulation section at time  $t$ , pair candidates  $f_1$  and  $f_2$  that satisfy the condition  $(f_{1prd}-\epsilon) < (f_1+f_2)/2 < (f_{1prd}+\epsilon)$  are acquired. Here,  $\epsilon$  represents a constant that is appropriately set based on a possible error.

(3) From among pairs acquired in processing (2), a pair candidate not including  $f_{2prd}$  that satisfies  $f_2-f_1 \approx f_{2prd}-$

flprd is excluded from the acquired pair candidates. Here, f2prd is a beat frequency in the downstream-modulation section at time  $t$ .

(4) From among pairs acquired in processing (3), one or more possible pairs are selected taken into consideration various other conditions used for pairing in an FMCW radar (the degree of coincidence between peak values of projecting portions appearing in frequency spectra, the degree of coincidence between peak directions obtained from profiles of angle directions of frequency spectra, and the like).

(5) In accordance with  $f_1$  and  $f_2$  selected in processing (4),  $f_r$  and  $f_d$  are calculated. The obtained results are substituted for conditions (4) and (6), and a relative distance  $R$  and a relative speed  $V$  are calculated.

An example in which the relative speed of a target differs from each other is shown in part (A) and (B) of Fig. 4. In both cases, a frequency component  $f_r$  based on a range delay at time  $t$  is substantially equal to a frequency  $f_1$  of an upbeat signal at time  $t-nT$ .

Fig. 5 shows an example of a change in a frequency  $f_1$  of an upbeat signal and a change in a frequency  $f_2$  of a downbeat signal when the target recedes from the radar. In this case,  $f_r$  at time  $t$  is substantially equal to  $f_1$  at time  $t-nT$ .

An example of a procedure for the above-described

pairing processing is shown as a flowchart in Fig. 6.

Here,  $t$  represents a variable indicating the number of measurement times. First, an initial value 0 is substituted for  $t$  (step S1). Sampling data of a beat signal is input, and an FFT arithmetic operation is performed (step S2 → step S3). Then, a peak frequency of a projecting portion appearing in a frequency spectrum of an upbeat signal (hereinafter, simply referred to as a "peak frequency of an upbeat signal") and a peak frequency of a projecting portion appearing in a frequency spectrum of a downbeat signal (hereinafter, simply referred to as a "peak frequency of a downbeat signal") that are calculated by the FFT arithmetic operation are substituted for two-dimensional array variables  $f1[t][ ]$  and  $f2[t][ ]$  (step S4). In the following descriptions, in order to collectively represent a data string of peak frequencies of a plurality of projecting portions appearing in frequency spectra of an upbeat signal and a downbeat signal at each timing, a one-dimensional array format is adopted.

Then, from among a plurality of peak frequencies included in the upbeat signal and the downbeat signal, a combination of peak frequencies  $f1[t]$  and  $f2[t]$  in which  $(f1[t]+f2[t])/2$  corresponds, within a range of  $\pm\epsilon$ , to a plurality of peak frequencies  $f1[t-nT]$  of an upbeat signal obtained by measurement performed  $nT$  times before is

extracted as a pair candidate (step S5).

Then, a combination of  $f1[t]$  and  $f2[t]$  not including  $f2[t-nT]$  in which a difference between the peak frequency  $f1[t]$  of the upbeat signal and the peak frequency  $f2[t]$  of the downbeat signal that are obtained at the current time is substantially equal to a difference ( $f2[t-nT]-f1[t-nT]$ ) between  $f1$  and  $f2$  at time  $t-nT$  is excluded from pair candidates (step S6). Then, the most appropriate combination is determined as a pair, taking into consideration the similarity of the peak intensity and the similarity of the peak direction (step S7).

Pairing at each measurement timing is performed by repeating the above-described processing (step S7  $\rightarrow$  step S8  $\rightarrow$  step S2  $\rightarrow$  ...).

Another processing operation for pairing in a radar according to a second embodiment of the present invention is described next with reference to Fig. 7.

Although  $fr$  at time  $t$  is estimated from  $f1$  and  $f2$  at time  $t-nT$  in the first embodiment,  $fr$  at time  $t-nT$  is estimated from  $f2$  at time  $t$  in the second embodiment.

Fig. 7 is a flowchart showing a processing procedure of the pairing operation. The processing procedure shown in Fig. 7 is different from the example shown in Fig. 6 in steps S15, S16, and S18. In step S15, from among a plurality of peak frequencies included in an upbeat signal

and a downbeat signal at time  $t-nT$ , a combination of peak frequencies  $f1[t-nT]$  and  $f2[t-nT]$  in which  $(f1[t-nT]+f2[t-nT])/2$  corresponds, within a range of  $\pm\epsilon$ , to a plurality of peak frequencies  $f2[t]$  of a downbeat signal obtained by the current measurement is extracted as a pair candidate.

Then, a combination of  $f1[t-nT]$  and  $f2[t-nT]$  not including  $f1[t]$  in which a difference  $(f2[t]-f1[t])$  between a peak frequency  $f1$  of an upbeat signal and a peak frequency  $f2$  of a downbeat signal at time  $t$  is substantially equal to a difference  $(f2[t-nT]-f1[t-nT])$  between  $f1$  and  $f2$  at time  $t-nT$  is excluded from pair candidates (step S16).

Then, the most appropriate combination is determined as a pair, taking into consideration the similarity of the peak intensity and the similarity of the peak direction (step S17).

Then, using the paired  $f1[t-nT]$  and  $f2[t-nT]$ ,  $f1[t]$  and  $f2[t]$  in which a Doppler shift frequency serving as a difference between  $f1$  and  $f2$  obtained by measurement at the current time is substantially equal to a Doppler shift frequency serving as a difference between  $f1$  and  $f2$  obtained by measurement at time  $t-nT$  (that is,  $f1[t]$  and  $f2[t]$  that satisfy the condition  $f2[t]-f1[t] \approx f2[t-nT]-f1[t-nT]$ ) are extracted, and a relative distance and a relative speed at the current measurement timing are calculated (step S18) from the following conditions:

$f_r[t] = (f_1[t] + f_2[t])/2$ ; and

$f_d[t] = (f_2[t] - f_1[t])/2$ .

A radar according to a third embodiment will be described with reference to Figs. 8 and 9.

Although cases where the measurement cycle  $T$  satisfies condition (11) are described in the first and second embodiments, a desired measurement cycle can be set in the third embodiment.

Fig. 8 shows an example of changes of a peak frequency  $f_1$  of an upbeat signal, a peak frequency  $f_2$  of a downbeat signal, and a frequency component  $f_r$  based on a range delay that are obtained at measurement timings. In this example, a cycle  $nT$  does not satisfy the condition  $nT \approx \tau$  even if  $n$  is appropriately selected such that a difference between  $nT$  and  $\tau$  is minimum, and the relationship  $nT < \tau$  is achieved. Thus,  $f_1$  at a previous measurement timing  $t - nT$  does not correspond to  $f_r$  at the current measurement timing  $t$ .

Fig. 9 is a flowchart showing a processing procedure for pairing in the radar according to the third embodiment. The processing procedure shown in Fig. 9 is different from the procedure shown in Fig. 6 in steps S25 to S27. In step S25,  $f_2$  at the current time  $t$  that is the nearest to  $f_1$  at time  $t - 2nT$  is selected, and  $f_1$  and  $f_2$  at time  $t - nT$  in which the average of  $f_1$  and  $f_2$  corresponds, within a range of  $\pm \epsilon$ , to  $f_r$  at time  $t - nT$  (that is,  $(f_1[t - 2nT] + f_2[t])/2$ ) are



extracted as a pair candidate.

Then, a combination of  $f_1[t-nT]$  and  $f_2[t-nT]$  not including  $f_1[t]$  in which a difference  $(f_2[t]-f_1[t])$  between a peak frequency  $f_1$  of an upbeat signal and a peak frequency  $f_2$  of a downbeat signal at time  $t$  is substantially equal to a difference  $(f_2[t-nT]-f_1[t-nT])$  between  $f_1$  and  $f_2$  at time  $t-nT$  is excluded from pair candidates (step S26).

In addition, similarly, a combination of  $f_1[t-nT]$  and  $f_2[t-nT]$  not including  $f_2[t-2nT]$  in which a difference  $(f_2[t-2nT]-f_1[t-2nT])$  between a peak frequency  $f_1$  of an upbeat signal and a peak frequency  $f_2$  of a downbeat signal at time  $t-2nT$  is substantially equal to a difference  $(f_2[t-nT]-f_1[t-nT])$  between  $f_1$  and  $f_2$  at time  $t-nT$  is excluded from pair candidates (step S27).

Accordingly,  $f_r$  at time  $t-nT$  is estimated from  $f_2$  at time  $t$  and  $f_1$  at time  $t-2nT$ , a pair in which a frequency component based on a range delay satisfies the estimated  $f_r$  is extracted as a pair candidate, and a combination of a pair in which a Doppler shift frequency that is substantially equal to a Doppler shift frequency component  $f_d[t-nT]$  calculated from the extracted pair exists at a measurement timing of time  $t$  or time  $t-2nT$  is extracted. Accordingly, a pair candidate at time  $t-nT$  is extracted.

In order to calculate  $f_r$  and  $f_d$  at time  $t$ , as in the processing of step S18 shown in Fig. 7,  $f_1[t]$  and  $f_2[t]$  in

which a Doppler shift frequency serving as a difference between  $f_1$  and  $f_2$  obtained by the current measurement is substantially equal to a Doppler shift frequency serving as a difference between  $f_1$  and  $f_2$  obtained by measurement at time  $t-nT$  (that is,  $f_1[t]$  and  $f_2[t]$  that satisfy the condition  $f_2[t]-f_1[t] \approx f_2[t-nT]-f_1[t-nT]$ ) are extracted using  $f_1[t-nT]$  and  $f_2[t-nT]$  regarded as being a pair, and a distance and a relative speed at the current measurement timing are calculated from the following conditions:

$$f_r[t] = (f_1[t]+f_2[t])/2; \text{ and}$$

$$f_d[t] = (f_2[t]-f_1[t])/2.$$